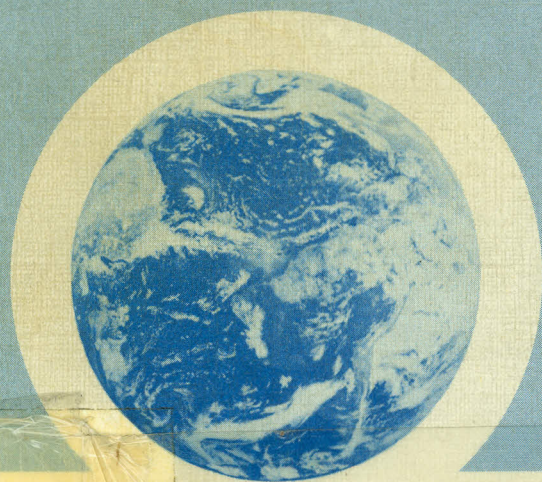


# **Atmospheric Turbulence and Air Pollution Modelling**

**Edited by  
F. T. M. Nieuwstadt and H. van Dop**



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# Atmospheric Turbulence and Air Pollution Modelling

*A Course held in The Hague,  
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edited by

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